

Geometry

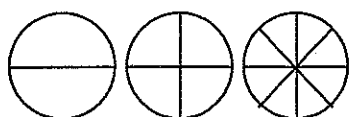
Notes 1-1 Patterns and Inductive Reasoning

Name KEY

Date _____ Period _____

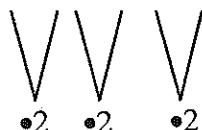
Inductive Reasoning:

What is the next pattern?



What are the next two terms?

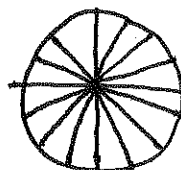
3, 6, 12, 24,



Inductive reasoning is reasoning that is based on patterns you observe.

If you observe a pattern in a sequence you can use inductive reasoning to tell what the next term in the sequence will be.

Draw the next pattern in the sequence:



Write the next two terms in the sequence:

48, 96

A Conjecture

Example:

Make a conjecture about the sum of the first 30 odd numbers.

Is a conclusion you reach using inductive reasoning (reasoning based on a pattern you observe.)

$$\begin{array}{rclcl} 1 & = 1 & = 1^2 & 1 \\ 1 + 3 & = 4 & = 2^2 & 2 \\ 1 + 3 + 5 & = 9 & = 3^2 & 3 \\ 1 + 3 + 5 + 7 & = 16 & = 4^2 & 4 \\ 1 + 3 + 5 + 7 + 9 & = 25 & = 5^2 & 5 \end{array}$$

Using inductive reasoning you can conclude that the sum of the first 30 odd numbers is 30^2 , or 900.

A Counter Example

Not all conjectures turn out to be true. You can prove a conjecture false by finding one counter example.

A counter example to a conjecture is an example for which the conjecture is incorrect.

Finding Counter Examples

$$\begin{aligned} 1^2 &= 1 \\ 2^2 &= 4 \\ 3^2 &= 9 \\ 4^2 &= 16 \\ 5^2 &= 25 \\ 6^2 &= 36 \\ 7^2 &= 49 \end{aligned}$$

Conjecture: The square of any number is greater than the original number.

Counter Example: $1^2 \nless 1$

Conjecture: Any three points can be connected to form a triangle.



Counter Example: If the three points are collinear they will not form a triangle.

You Try!

Find the next two terms:

1. 5, 10, 20, 40, 80, 160

2. 1, -1, 2, -2, 3, -3, 4

3.



4. Develop an algebraic expression which can be used to find how many square units will be in the n th figure if the pattern continues.

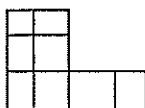


Figure 1

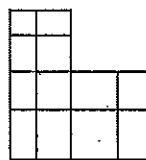


Figure 2

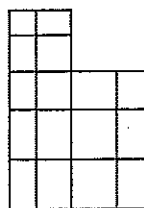


Figure 3

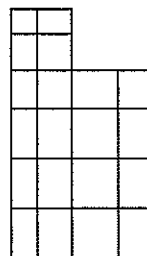


Figure 4

$n=1$
8

$n=2$
12

$n=3$
16

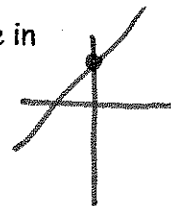
$n=4$
20

of square units

algebraic expression is

$4n + 4$

$y = mx + b$
 $y = 4x + 4$



0	4
X	Y
1	8
2	12
3	16
4	20

STAT
EDIT

-entered values
2nd Quit
STAT → CALC
4. LinReg